

*Answer any FIVE Questions
All Questions carry Equal Marks*

1. State and prove following properties of DTFT,
 - (i) Periodicity
 - (ii) Time-shifting
 - (iii) Multiplication by 'n' in time domain.

2. (a) Show that DFS of periodic sequences $x_p(n)$ is periodic with same period.
(b) State and prove duality property of DFS.

3. Write short notes on the following,
 - (i) Butterfly computation
 - (ii) Goertzel algorithm
 - (iii) In-place computations
 - (iv) Bit reversal

4. Obtain the direct form realization of following system functions with minimum number of multipliers
 - (i) $H(z) = (1/2) + (1/4)z^{-1} + (1/4)z^{-2} + (1/2)z^{-3}$.
 - (ii) $H(z) = [(1-z^{-1}) [(1/2) - (1/4)z + (1/2)z^2]]$

5. (a) Compare the backward and forward difference methods of digital filter approximations.
(b) Convert following analog filter transfer function into digital filter transfer function using backward difference method $H(s) = 1/(s+2)^2 + 16$.

6. (a) Explain characterization of FIR filters.
(b) Sketch and explain the frequency response of non-ideal digital highpass filter.

7. The signal $x(n)$ is up sampled by factor 2, then it is passed through ideal low pass filter with cutoff frequency of F_c and down sampled by factor by 3. Sketch the input and output spectrum for the case $X(F) = \text{tri}(4F)$ with $F_c = 0.15$.

8. (a) Discuss about spectral analysis of sinusoidal signals.
(b) With necessary block diagrams explain about discrete multi tone receiver.